2018-00646 - PhD Position/ Swimming for low Reynolds numbers [S]

Level of qualifications required: Graduate degree or equivalent
Function: PhD Position

Context

Team

Contacts
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Assignment

Context

The swimming problem consists in controlling the rigid displacement of a (deformable) object placed in a fluid. In order to move the object, one acts on controls which are the (non-rigid) deformations of the object. The equations connecting the rigid deformation to the non-rigid deformation are obtained by a coupling between the partial differential equations modeling the motion of the fluid (the Navier-Stokes equations) and the fundamental principle of the dynamics (Newton's laws), describing the rigid motion of the swimmer. These two systems are coupled by the continuity of the velocities at the swimmer's boundary. The corresponding system is considered as a control system where the input of the system is the deformation imposed on the swimmer and the output is the position and orientation of the swimmer. Several theoretical studies of this problem have been carried out in the limiting cases of low Reynolds numbers or high Reynolds number. In these cases, one can approach the Navier-Stokes equations by the Stokes equations or by a Poisson problem (potential fluid), and in some cases one can obtain explicit formulas of the solution of the system.

Main activities

Project description

The low-Reynolds number problem was considered experimentally by Taylor in the 1950s and several works were done by Purcell, Childress, Shapere and Wilczek, etc. More recently one can mention the work of Chambrion and Munnier for the high Reynolds numbers and that of Alouges, DeSimone et al. for the low Reynolds numbers.

A first line of research will consist of extending and improving existing commandability results. It has been shown that generically only four independent deformations are enough to control an isolated swimmer surrounded by a fluid. A first objective of the thesis would be to reduce the number of controls. This can be done by computing high order Lie brackets. In a second time, it will be possible to look at the case where the swimmer is confined in a bounded cavity. It was noted in previous works that the boundary of this cavity could play a role in the swimming mechanism. The last extension could be to generalize the controllability results on the low Reynolds swimmers to the case of the Navier-Stokes system for the fluid.

A second line of research will be to understand the structure of the optimal swimming. Given the physical nature of the system considered, it is natural to impose constraints on the swimmer's deformation and speed of deformation. Typically, we will assume that the control is bounded and that the deformation parameters belong to a compact set.
These constraints induce the existence of a minimum control time to send the swimmer to a prescribed target. The object is to better understand this minimum time function and the structure of time optimal controls (periodicity, regularity, etc).

Finally the last axis of the thesis will focus on the validation of the theoretical results by numerical simulations. This will allow us in particular to support our intuition in many cases where we are not able to rigorously demonstrate some results. This requires first to develop a rapid numerical method for solving the direct problem where the swimming mechanism is prescribed (without specifying a position objective). In the limit case of low Reynolds numbers, it is possible to consider boundary integral methods, whose interests are the computational speed and the accuracy of the swimmer's geometry. However, this method is difficult to generalize in the other cases. Once the direct problem has been implemented, it will be necessary to focus on the minimization of a cost (optimal control problem). Solving such problems is usually difficult to implement. A strategy can be the use of homotopy methods in order to take advantage of our good understanding of the limit case of low Reynolds numbers.

**Skills**

**Required qualifications**

MSc in mathematics

**Language**

French or English.

**Benefits package**

- Subsidised catering service
- Partially-reimbursed public transport
- Social security
- Paid leave
- French courses

**Remuneration**


Monthly salary after taxes: around 1596,05€ for 1st and 2nd year. 1678,99€ for 3rd year. (medical insurance included).

**General Information**

- **Theme/Domain**: Optimization and control of dynamic systems
  Scientific computing (BAP E)
- **Town/city**: Villers-lès-Nancy
- **Inria Center**: CRI Nancy - Grand Est
- **Starting date**: 2018-10-01
- **Duration of contract**: 3 years
- **Deadline to apply**: 2018-05-01

**Contacts**

- **Inria Team**: SPHINX
- **Recruiter**: Takahashi Takéo / takeo.takahashi@inria.fr

**The keys to success**

**Application deadline**
May 1st, 2018 (Midnight Paris time)

How to apply

Upload your file on jobs.inria.fr in a single pdf or zip file, and send it as well by email to takeo.takahashi@inria.fr. Your file should contain the following documents:

- Your CV.
- A cover/motivation letter describing your interest in this topic.
- A short (max one page) description of your Master thesis (or equivalent) or of the work in progress if not yet completed.
- Your degree certificates and transcripts for Bachelor and Master (or the last 5 years).
- Master thesis (or equivalent) if it is already completed and publications if any (it is not expected that you have any). Only the web links to these documents are preferable, if possible.

In addition, one recommendation letter from the person who supervises(d) your Master thesis (or research project or internship) should be sent directly by his/her author to takeo.takahashi@inria.fr.

Applications are to be sent as soon as possible.

Conditions for application

Defence Security:
This position is likely to be situated in a restricted area (ZRR), as defined in Decree No. 2011-1425 relating to the protection of national scientific and technical potential (PPST). Authorisation to enter an area is granted by the director of the unit, following a favourable Ministerial decision, as defined in the decree of 3 July 2012 relating to the PPST. An unfavourable Ministerial decision in respect of a position situated in a ZRR would result in the cancellation of the appointment.

Recruitment Policy:
As part of its diversity policy, all Inria positions are accessible to people with disabilities.

Warning: you must enter your e-mail address in order to save your application to Inria. Applications must be submitted online on the Inria website. Processing of applications sent from other channels is not guaranteed.