The thesis will be carried out within the INOCS team whose primal goal is the study of optimization problems involving complex structures. The scientific objectives of INOCS are related to modeling and methodological concerns. The INOCS team focuses on integrated models for problems with complex structure (CS) taking into account the nature and the structure of the decisions as well as the properties of the problem.
The thesis will be supervised by Martine Labbé whose expertise concerns the resolution of bilevel problems using mixed integer linear models and who focuses in particular on pricing optimisation problems.

More information: https://www.inria.fr/equipes/inocs

**Mission confiée**

**Research project**

The first part of this doctoral research project will be devoted to the development of price optimization models to tackle the Rank Pricing Problem. This problem aims at setting the prices of the products of a company taking into account that we deal with unit-demand customers whose rule selection of products is based on preferences. Due to the hierarchical structure of the problem, it will be modelled as a bilevel program. In the first place, unlimited supply will be considered.

The problem will be formulated as a bilevel program and then transformed into a single level optimisation problem with a nonlinear objective. Different linearization techniques will lead to several formulations to compare and the polyhedral structure of the resulting models will be studied. From the bilevel formulations, several single level formulations might be developed and strengthening valid inequalities should be derived. Furthermore, the efficiency of the proposed formulations will be evaluated through an extensive computational study.

Afterwards, the problem will be generalised by considering limited supply. This will lead to new formulations, since the items must the allocated to the customers.

**State of the art**

Price setting problems stated using bilevel programming fit multiple applications in sectors such as networks (an overview can be found in [1]), the trucking industry and in the context of air traffic management, to cite but a few.

Rusmevichientong et al.[2] are the first to propose maximum and minimum utility objectives, as well as a rank-buying objective for pricing problems with unlimited supply and unit-demand customers. In the first two cases, the customer purchases the item which maximizes or minimizes the difference between his budget and the price of the product, whereas in the rank-buying objective the client buys the product that ranks highest and he can afford. In this case, the authors represent a customer by its budget and an ordered list of recommended products, and capture his purchasing behaviour by means of a choice function. They show that these problems are NP-complete in the strong sense and propose a heuristic approximation algorithm. Variations of the model are considered in [3]. The optimal resolution of these problems by means of Integer Programming techniques has not yet been approached in the literature.

**References**


**Principales activités**

**Main activities:**

- Develop bilevel and mixed integer models for rank pricing problems.
- Compare models from theoretical and computational points of view.
- Carry out polyhedral studies of ranks pricing problems.
- Develop solution algorithms based on the previous findings using cutting plane or column generation approaches.
- Carry out computational experiments to determine the best solution approach.

**Additional activities:**

- write scientific reports and articles.
- Give presentation at scientific meetings.

**Compétences**
**Skills**

Candidates should hold a Master's degree in Operations research, mathematics, computer science, or similar fields and should ideally have a solid background in discrete optimization, integer programming, decomposition techniques. Computer science skills in algorithmic and C/C++ development are also welcome.

Knowledge of French is not required, but good communication skills and a solid knowledge of English are essential.

**Avantages sociaux**

**Benefits**

- Subsidised catering service
- Partially-reimbursed public transport
- Social security
- Paid leave
- Sports facilities
- Flexible working hours

More information about Lille:

http://www.lille3000.eu/portail/
http://www.lillemetropole.fr/mel.html

**Rémunération**

**Remunerating**

The gross monthly salary is 1982€ for the 1st and the 2nd year, 2085€ for the 3rd year