

## 2019-01307 - PhD Position F/M Numerical modelling of coupled liquid gas Darcy flow and mechanical deformation in fractured porous media

Type de contrat : CDD de la fonction publique  
Niveau de diplôme exigé : Bac + 5 ou équivalent  
Fonction : Doctorant

### A propos du centre ou de la direction fonctionnelle

The Inria Sophia Antipolis - Méditerranée center counts 37 research teams and 9 support departments. The center's staff (about 600 people including 400 Inria employees) is composed of scientists of different nationalities (250 foreigners of 50 nationalities), engineers, technicians and administrators. 1/3 of the staff are civil servants, the others are contractual. The majority of the research teams at the center are located in Sophia Antipolis and Nice in the Alpes-Maritimes. Six teams are based in Montpellier and a team is hosted by the computer science department of the University of Bologna in Italy. The Center is a member of the University and Institution Community (ComUE) "Université Côte d'Azur (UCA)".

### Contexte et atouts du poste

The PhD proposal is part of a project in collaboration between Andra, Monash University and l'Université Côte d'Azur (laboratoire de Mathématiques J.A. Dieudonné (LJAD) and joint LJAD-Inria team Coffee). The PhD will be co-supervised by Roland Masson, Laurent Monasse, Konstantin Brenner from joint LJAD-Inria team Coffee and by Laurent Trenty from Andra. Jérôme Droniou, from the department of Mathematics of Monash University, Melbourne, Australia, will also be involved in this project. The PhD will be held at LJAD on the Campus of Valrose in Nice with periodic meetings with Andra and also includes stays at Monash University.

### Mission confiée

Many real life applications in the geosciences involve processes like multi-phase flow and hydro-mechanical coupling in heterogeneous porous media. Such mathematical models are coupled systems of partial differential equations, including nonlinear and degenerate parabolic ones. Next to the inherent difficulties posed by such equations, further challenges are due to the heterogeneity of the medium and the presence of discontinuities like fractures. This has a strong impact on the complexity of the models, challenging their mathematical and numerical analysis and the development of efficient simulation tools.

This PhD project focuses on the so called hybrid-dimensional matrix fracture models obtained by averaging both the unknowns and the equations in the fracture width and by imposing appropriate transmission conditions at both sides of the matrix fracture interfaces. Given the high geometrical complexity of real life fracture networks, the main advantages of these hybrid-dimensional compared with full-dimensional models are to both facilitate the mesh generation and the discretisation of the model, and to reduce the computational cost of the resulting schemes. This type of hybrid-dimensional models has been the object of intensive researches since the last 15 years due to the ubiquity of fractures in geology and their considerable impact on the flow and transport of mass and energy in porous media, and on the mechanical behavior of the rocks.

The application targeted in this PhD deals with the simulation of the liquid gas transient flow coupled with the rock mechanical deformation in the deep Collovo-Oxfordian geological storage studied by Andra.

The fracture network is initially induced by the drilling of the underground tunnels resulting in a damaged zone in the neighbourhood of the excavated galleries with fractures of variable connectivity, sizes and widths. The objective is to study the impact of the gas pressure on the width of the fractures and finally on the homogenized permeability and porosity at the scale of the damaged zone.

Hybrid-dimensional matrix fracture models combine geometrical complexity with highly contrasted properties and constitutive laws at the matrix fracture interfaces leading to strong nonlinear couplings and a large range of space and time scales. It leads to new challenges in terms of mathematical analysis, discretization and nonlinear solvers. We will consider hydro-mechanical models that couple the hybrid-dimensional porous media liquid gas flow with the rock mechanical deformation. For such models, the flow in the fractures has a strong nonlinear dependence upon the fracture width, resulting from the rock mechanical deformation which itself depends on the fluid pressure in the fractures. This type of models involves many challenges, some of which are listed here. First, the mathematical formulation of the problem involves weighted spaces with weights which depend on the unknown fracture width. The discretization should also find a compromise between robustness, accuracy and cost, while being able to adapt to heterogeneities. The numerical scheme should ensure conservation and avoid locking and inf-sup instabilities. At the tip of the fractures, the mechanical stress exhibits singularities which should be resolved. This is especially important in the case when the fractures propagate, since their dynamics is driven by the crack tip stress concentration. The convergence analysis is hindered by the severe non-linearities, and similarly, the fully nonlinear schemes are difficult to solve.

### Bibliography:

Martin, V., Jaffré, J., Roberts, J. E., Modeling fractures and barriers as interfaces for flow in porous media, SIAM J. Sci. Comput. 26 (5), 1667-1691, 2005.

K. Brenner, J. Hennicker, R. Masson, P. Samier, Gradient Discretization of Hybrid Dimensional Darcy Flows in Fractured Porous Media with discontinuous pressure at matrix fracture interfaces. IMA Journal of Numerical Analysis, 27 september 2016. <https://hal.archives-ouvertes.fr/hal-01192740>.

J. Aghili, K. Brenner, J. Hennicker, R. Masson, L. Trenty, Two-phase Discrete Fracture Matrix models

### Informations générales

- **Thème/Domaine :** Schémas et simulations numériques  
Calcul Scientifique (BAP E)
- **Ville :** Nice
- **Centre Inria :** CRI Sophia Antipolis - Méditerranée
- **Date de prise de fonction souhaitée :** 2019-09-01
- **Durée de contrat :** 3 ans
- **Date limite pour postuler :** 2019-06-30

### Contacts

- **Equipe Inria :** COFFEE
- **Directeur de thèse :**  
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### A propos d'Inria

Inria, l'institut national de recherche dédié aux sciences du numérique, promeut l'excellence scientifique et le transfert pour avoir le plus grand impact. Il emploie 2400 personnes. Ses 200 équipes-projets agiles, en général communes avec des partenaires académiques, impliquent plus de 3000 scientifiques pour relever les défis des sciences informatiques et mathématiques, souvent à l'interface d'autres disciplines. Inria travaille avec de nombreuses entreprises et a accompagné la création de plus de 160 start-up. L'institut s'efforce ainsi de répondre aux enjeux de la transformation numérique de la science, de la société et de l'économie.

### Consignes pour postuler

#### Sécurité défense :

Ce poste est susceptible d'être affecté dans une zone à régime restrictif (ZRR), telle que définie dans le décret n°2011-1425 relatif à la protection du potentiel scientifique et technique de la nation (PPST). L'autorisation d'accès à une zone est délivrée par le chef d'établissement, après avis ministériel favorable, tel que défini dans l'arrêté du 03 juillet 2012, relatif à la PPST. Un avis ministériel défavorable pour un poste affecté dans une ZRR aurait pour conséquence l'annulation du recrutement.

#### Politique de recrutement :

Dans le cadre de sa politique diversité, tous les postes Inria sont accessibles aux personnes en situation de handicap.

**Attention :** Les candidatures doivent être déposées en ligne sur le site Inria. Le traitement des candidatures adressées par d'autres canaux n'est pas garanti.

with linear and nonlinear transmission conditions, accepted in International Journal on Geomathematics, 2019. <https://hal.archives-ouvertes.fr/hal-01764432>.

K. Brenner, J. Hennicker, R. Masson, P. Samier, Hybrid Dimensional Modelling of Two-phase Flow through fractured with enhanced matrix fracture transmission conditions, Journal of Computational Physics, volume 357, pages 100-124, march 2018. <https://hal.archives-ouvertes.fr/hal-01584887>.

V. Girault, M.F. Wheeler, B. Ganis, M.E. Mear. A lubrication fracture model in a poro-elastic medium, M3AS, 2014.

Hanowski, K.K., Sander, O.: Simulation of Deformation and Flow in Fractured, Poroelastic Materials (2016). URL <http://arxiv.org/abs/1606.05765>

E. Ucar, I. Berre, E. Keilegavlen, Three Dimensional Numerical Modeling of Shear Stimulation of Fractured Reservoirs, Journal of Geophysical Research: Solid Earth, 2018.

L. Beaudé, R. Masson, S. Lopez, P. Samier, Combined face based and nodal based discretizations on hybrid meshes for non-isothermal two-phase Darcy flow problems, preprint 2018, <https://hal.archives-ouvertes.fr/hal-01832659>

J. Droniou, R. Eymard, T. Gallou{"e"}, C. Guichard, and R. Herbin, The gradient discretisation method. Mathematics and Applications, vol. 82. Springer, 2018, 511p. doi:10.1007/978-3-319-79042-8. <https://hal.archives-ouvertes.fr/hal-01382358>.

J. Droniou, J. Hennicker, R. Masson, Numerical Analysis of a Two-Phase Flow Discrete Fracture Model, Numerische Mathematik online september 2018. <https://hal.archives-ouvertes.fr/hal-01422477>.

## Principales activités

This PhD project will investigate time splitting and nonlinear solver strategies to solve the strong nonlinear coupling between the liquid gas Darcy flow and the rock mechanical deformation. It will also explore spatial discretizations combining a nodal approximation of the flow and mechanical models in the matrix with a face based approximation in the fractures and at the matrix fracture interfaces. This will provide both the locality of the transmission conditions at the matrix fracture interfaces and a low number of degrees of freedom on simplicial meshes. An essential enabler of the convergence analyses carried out on the schemes designed during the PhD project lies in the series of works around discrete functional analysis (current topic of the Australian Research Council-funded project of J. Droniou), and in particular its application to fully non-linear and possibly degenerate models.

## Compétences

Applicant should have a Master degree in applied mathematics with a good knowledge of the discretization of partial differential equations. She/he should be familiar with a scientific programming language such as Fortran, C or C++, have a first experience in scientific computing and be interested in physics and team working.

## Avantages

- Subsidized meals
- Partial reimbursement of public transport costs
- Leave: 7 weeks of annual leave + 10 extra days off due to RTT (statutory reduction in working hours) + possibility of exceptional leave (sick children, moving home, etc.)
- Possibility of teleworking (after 6 months of employment) and flexible organization of working hours
- Professional equipment available (videoconferencing, loan of computer equipment, etc.)
- Social, cultural and sports events and activities
- Access to vocational training
- Social security coverage

## Rémunération

Monthly gross salary : 1st and 2nd year : 1.982 euros

Monthly gross salary : 3rd year : 2.085 euros