Primal-Dual relaxations for Non-Linear Problems

Contract type: Fixed-term contract
Renewable contract: Yes
Level of qualifications required: PhD or equivalent
Function: Post-Doctoral Research Visit
Level of experience: From 3 to 5 years

About the research centre or Inria department

The Inria centre at Université Côte d'Azur includes 37 research teams and 8 support services. The centre's staff (about 500 people) is made up of scientists of different nationalities, engineers, technicians and administrative staff. The teams are mainly located on the university campuses of Sophia Antipolis and Nice as well as Montpellier; in close collaboration with research and higher education laboratories and establishments (Université Côte d'Azur; CNRS, INRAE, INSERM…), but also with the region's economic players.

With a presence in the fields of computational neuroscience and biology, data science and modeling, software engineering and certification, as well as collaborative robotics, the Inria Centre at Université Côte d'Azur is a major player in terms of scientific excellence through its results and collaborations at both European and international levels.

Context

Team AROMATH (https://team.inria.fr/aromath/), Inria at Université Côte d'Azur; team leader Bernard Mourrain

Research topics: computational algebraic geometry; efficient algorithms for solving the non-linear problems, exploiting algebraic structures, stable against numerical perturbation; high order geometric modeling exploiting algebraic representations, for the accurate description of shapes.

Contact: Bernard Mourrain (http://www-sop.inria.fr/members/Bernard.Mourrain/)

Besides carrying out high quality research, we expect the postdoc to participate to the activities of the EU network TENORS on tensors and optimisation, which will start in January 2024.

The postdoc will also have the opportunity to collaborate with PhD students working on related topics.

Assignment

Non-Linear Equations are ubiquitous in domains such as geometric modelling, scientific computing, data analysis, … Finding their solutions is an instance of non-linear optimisation problems. A classical approach to tackle these non-linear problems is to use local methods, such as Newton method or gradient descent methods. This family of methods is widely used in practice, but it only provides local extrema with no guaranty for a global solution. Moreover, it is very sensitive to the choice of the initial point. Alternative algebraic approaches such as Gröbner basis have been developed over the last decades to compute all the solutions of polynomial equations [2]. They involve direct computations with the polynomial equations, but are not numerically stable. Border basis [6], which have been developed more recently for robustness purposes, also involves primal polynomial computations.

At the turn of this century, an innovative approach has been proposed by J.B. Lasserre, to approximate global optima [4]. It involves primal convex cones of sums of squares of polynomials and their dual cones of pseudo-moment sequences. The core of the approach is to approximate positive polynomials by sums of squares and moments of measures by positive pseudo-moment sequences. These primal-dual relaxations allow to recover the optimal value and all the solutions of the optimization problem.

The objective of the project is to explore new types of primal-dual relaxations, which lead to efficient methods for solving global non-linear problems.

The first part of the project will be dedicated to the study of non-linear problems with a finite number of solutions, based on linear primal and dual relaxations. We will investigate new methods extending the Truncated Normal Form (TNF) approach [5] for solving non-linear constraints.

In a second part, we will consider non-linear optimisation problems defined on general basic semi-algebraic sets. We will investigate new primal and dual convex relaxations for other types of functions such as splines, polynomial exponential functions [3], or network functions used in Machine Learning for data fitting. We aim at analysing the capacity of approximation of these relaxations [1], their potential to recover the network functions used in Machine Learning for data fitting. We aim at analysing the capacity of approximation of these relaxations [1], their potential to recover the network functions used in Machine Learning for data fitting.

References


About Inria

Inria is the French national research institute dedicated to digital science and technology. It employs 2,600 people. Its 200 agile project teams, generally run jointly with academic partners, include more than 3,500 scientists and engineers working to meet the challenges of digital technology, often at the interface with other disciplines. The Institute also employs numerous talents in over forty different professions. 900 research support staff contribute to the preparation and development of scientific and entrepreneurial projects that have a worldwide impact.

General Information

• Theme/Domain: Algorithmics, Computer Algebra and Cryptology
• Town/city: Sophia Antipolis
• Inria Center: Centre Inria d’Université
  Côte d’Azur
• Starting date: 2023-10-01
• Duration of contract: 1 year
• Deadline to apply: 2023-12-30

Contacts

Inria Team: AROMATH
Recruiter: Mourrain Bernard /
Bernard.Mourrain@inria.fr

The keys to success

Candidates must hold a PhD in Mathematics or Computer Sciences. Candidates must also show evidence of research productivity (e.g. papers, conference presentations, etc.) at the highest level.

We prefer candidates who have strong mathematical background (on computer algebra, optimisation or scientific computing) and in general are keen on using mathematics to model real problems and get insights. The candidate should also be knowledgeable on software development and have good programming skills. Previous experiences with Julia is a plus.

The position is for 12 months, renewable for one more year, for a total of 24 months.

Warning: you must enter your e-mail address in order to save your application to Inria. Applications must be submitted online on the Inria website. Processing of applications sent from other channels is not guaranteed.
Main activities
The research activity will follow a classical path: literature review, exchange, brainstorming, development of new results...
Software development (for instance with Julia Language) and experimentation can be considered to validate new methods. The collaboration will be conducted through regular meetings with the advisors.
The post-doctoral fellow will have the opportunity to bring his/her own expertise and will be encouraged to open up his/her own research avenues.
He/she will benefit from the rich environment and expertise in effective algebraic geometry and computer algebra at the AROMATH team and at the University Côte d'Azur, from seminars and workshops and from our network of collaborators.

Skills
The following skills are desired for this position:
- a strong research background in the domain of the project (or at least in a specific area such as computer algebra, geometry, optimization or scientific computing)
- good communication and reporting skills, and an interest in collaborative work
- proficiency in English

Benefits package
- Subsidized meals
- Partial reimbursement of public transport costs
- Leave: 7 weeks of annual leave + 10 extra days off due to RTT (statutory reduction in working hours) + possibility of exceptional leave (sick children, moving home, etc.)
- Possibility of teleworking and flexible organization of working hours
- Professional equipment available (videoconferencing, loan of computer equipment, etc.)
- Social, cultural and sports events and activities
- Access to vocational training
- Contribution to mutual insurance (subject to conditions)

Remuneration
Gross Salary: 2746 € per month